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**Algorithm 1:** Proposed parallel prefix sum algorithm.
 

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**Input:** An array  $\vec{X} = (x_0, x_1, \dots, x_{n-1})$  of  $n$  numbers; number  $p$  of processors.

**Output:** Partial sums  $x_0, \Sigma_{x_0}^1, \Sigma_{x_0}^2, \dots, \Sigma_{x_0}^{x_{n-1}}$  of all the numbers in  $\vec{X}$ .

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1 begin
2   Divide  $\vec{X}$  into  $p$  equal-lengthed segments,  $\vec{S}_0, \vec{S}_1, \dots, \vec{S}_{p-1}$ .
   Assume the number of elements in  $\vec{S}_i$  is  $m$ , and  $m = \lfloor n/p \rfloor$  if
    $i \neq p-1$ , or  $m = n - \lfloor n(n-1)/p \rfloor$  if  $i = p-1$ .
3   Assign  $\vec{S}_i$  to processor  $p_i$ ,  $i \in [0, p-1]$ .
4   forall  $\vec{S}_i = (x_{i,0}, x_{i,1}, \dots, x_{i,m-1})$  in parallel do
5     for  $j \rightarrow 1$  to  $m-1$  do
6        $x_{i,j} = x_{i,j} + x_{i,j-1}$ 
7   for  $i \rightarrow 1$  to  $p-1$  do
8     Divide numbers in  $\vec{S}_i = (x_{i,0}, x_{i,1}, \dots, x_{i,m-1})$  into  $p$ 
     equal-lengthed segments,  $\vec{S}_{i,0}, \vec{S}_{i,1}, \dots, \vec{S}_{i,p-1}$ . Assume the
     number of elements in  $\vec{S}_{i,j}$  is  $w$ ,  $j \in [0, p-1]$ .
9     Assign  $\vec{S}_{i,j}$  to processor  $p_j$ ,  $j \in [0, p-1]$ .
10    forall  $\vec{S}_{i,j} = (x_{i,j,0}, x_{i,j,1}, \dots, x_{i,j,w-1})$  in parallel do
11      for  $k \rightarrow 0$  to  $w-1$  do
12         $x_{i,j,k} = x_{i,j,k} + x_{i-1,m-1}$  /*  $x_{i-1,m-1}$  is the
        last number in segment  $\vec{S}_{i-1}$  */
13 end
  
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