

(1)

$$\therefore 2b [T \sin \theta + 2W (\cos^2 \theta - \sin^2 \theta)] \sin \theta = 0$$

$$\therefore \sin \theta \neq 0$$

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$$\begin{aligned} \therefore T &= \frac{2W (\sin^2 \theta - \cos^2 \theta)}{\sin \theta} \\ &= \frac{2W (1 - 2\cos^2 \theta)}{\sqrt{1 - \cos^2 \theta}} \end{aligned}$$

$$\therefore BD = a \quad \text{so} \quad BO = \frac{a}{2}$$

$$\Rightarrow \cos \theta = \frac{BO}{AB} = \frac{a/2}{b} = \frac{a}{2b}$$

$$\therefore T = \frac{2W \left\{ 1 - 2 \left( \frac{a^2}{4b^2} \right) \right\}}{\sqrt{1 - \frac{a^2}{4b^2}}}$$

$$\boxed{T = \frac{2W \{2b^2 - a^2\}}{b \sqrt{4b^2 - a^2}}}$$

Q(2) Weights  $W_1, W_2$  are fastened to a light inextensible string ABC at the points B, C, the end A being fixed. Prove that, if a horizontal force P is applied at C and in equilibrium AB, BC are inclined at angles  $\theta, \phi$  to the vertical, then

$$P = (W_1 + W_2) \tan \theta = W_2 \tan \phi.$$