

* GAS TURBINE *

Advantage of Gas Turbine over I.C. engine →

1. High speed can be obtained
2. Easy Balancing.
3. They are compact. ($\frac{W}{P}$) [weight to power ratio is less]
4. Simple mechanism.

Disadvantage →

- 1) As compressor is used in gas turbine system the work of compression is large and hence net work is less this results in lower efficiency.
- 2) As gas turbine system are subjected to higher temp. continuously. high heat resistant costly material is required.
- 3) Additional Reduction gear box is required as the speeds are very high.

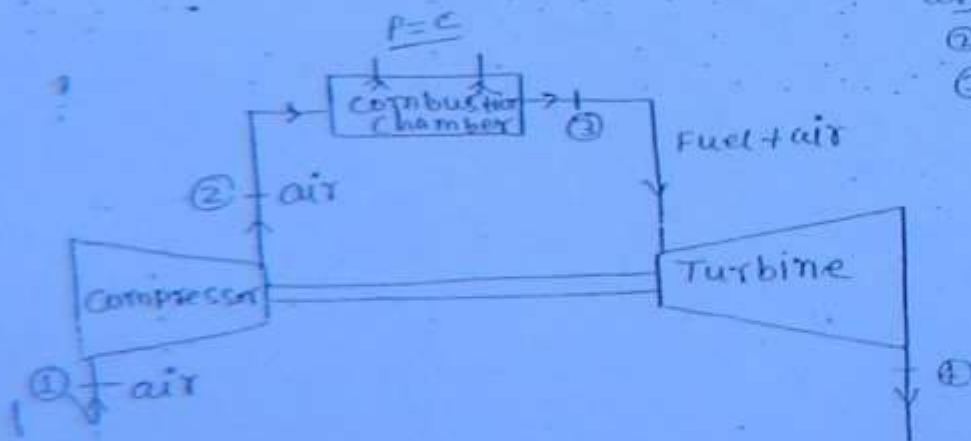
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Open cycle gas turbine → ^{WORKS ON} ~~cycle~~ (Joule / Brayton cycle)

application → Aircraft.

② automotive (bus and truck)

③ industrial gas turbine installation.

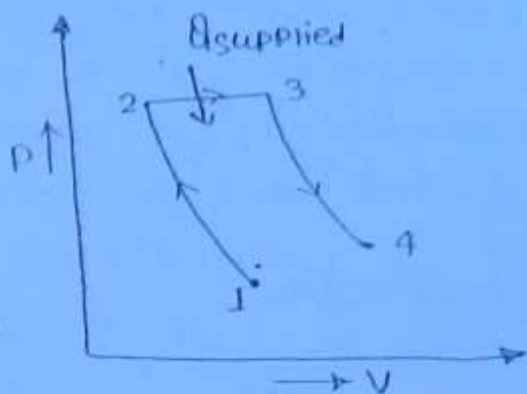


I.C. engine
Called

1-2 → Reversible adiabatic compression (Isentropic)

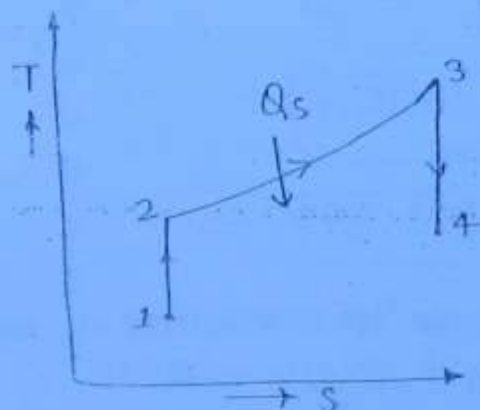
2-3 → Constant pressure heat addition

3-4 → Rev. adiabatic expansion. (Isentropic)



$$pV = \gamma RT$$

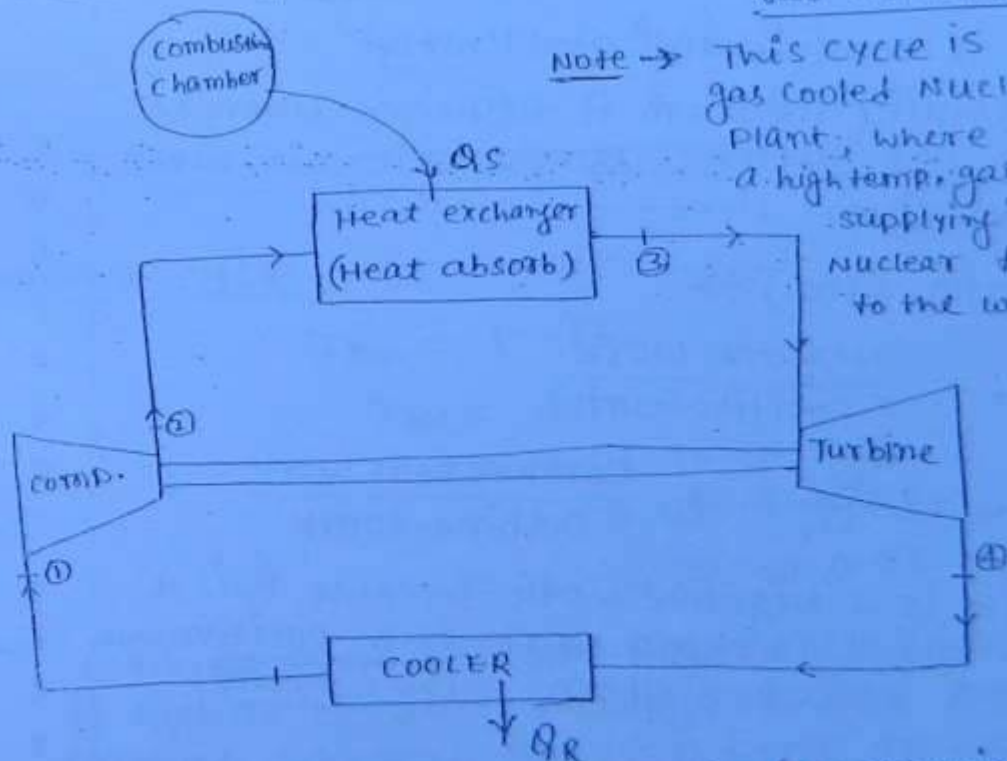
$$V \propto T$$



Note $\Rightarrow$ The Brayton cycle is the air standard cycle for the gas turbine power plant.

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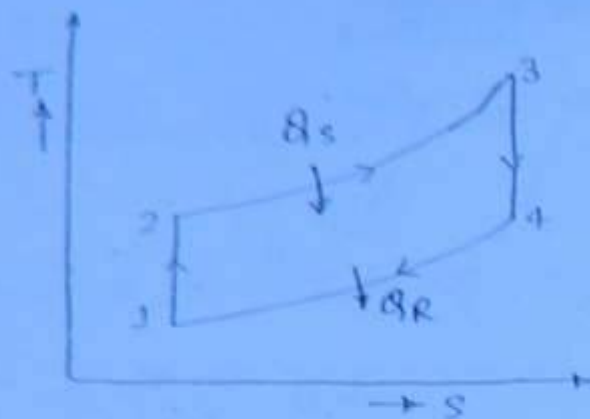
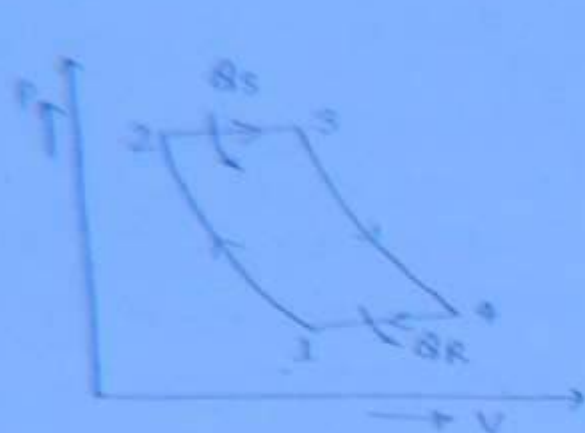
② closed cycle gas turbine $\Rightarrow$ ① Two Reversible isobars and two reversible adiabatic



Note $\rightarrow$ This cycle is used in a gas cooled nuclear reactor plant, where the source is a high temp. gas cooled reactor supplying heat from nuclear fission directly to the working fluid (a gas).

⊗ External Combustion Engine

- 1-2 $\rightarrow$ Rev. adiabatic compression (Isentropic)
- 2-3 $\rightarrow$ Constant pressure heat addition (Isobar)
- 3-4 $\rightarrow$ Rev. adiabatic expansion (Isentropic)
- 4-1 $\rightarrow$ Constant pressure heat rejection.



(BRAYTON CYCLE)

1 Gas Turbine cycle work on Brayton cycle.

Advantage of closed cycle gas turbine $\Rightarrow$

- 1) It can work on any working fluid but open cycle gas turbine must work on air only.
- 2) any cheaper fuel can be used because the product of combustion do not come directly in contact with turbine blade.

Disadvantages $\Rightarrow$

- 1) The system is complicated and costly
- 2) Additional cooling medium is required, whereas an open cycle gas turbine atmospheric air work as a cooling medium.

Back work Ratio (γ_{bw}) $\Rightarrow$

$$\gamma_{bw} = \frac{\text{Negative work}}{\text{Positive work}}$$

$$\gamma_{bw} = \frac{W_C}{W_T} \Rightarrow \frac{\text{Compressor work}}{\text{Turbine work}}$$

compressor work is a Negative work because it is a open system whereas Turbine work is a Positive work because this is a closed system $[W_C = -\int v dp]$

- 1) It is the ratio of Negative work to the Positive work.

In case of gas Turbine Power Plant the Back work ratio are around 40 to 60%, whereas in the case of Steam Power Plant (vapour power cycle / Rankine cycle) the Back work ratio are 1 to 2%.

⊕ WORK Ratio (R_w) ⇒

$$\gamma_w = \frac{\text{Net work}}{\text{Turbine work}} = \frac{W_{\text{net}}}{+ve \text{ work}} \Rightarrow \frac{W_{\text{net}}}{W_T}$$

$$\gamma_w = \frac{W_T - W_C}{W_T}$$

$$\gamma_w = 1 - \frac{W_C}{W_T}$$

$$\text{because } \gamma_{bw} = \frac{W_C}{W_T}$$

$$\gamma_w = 1 - \gamma_{bw}$$

⊕ The work ratio of Rankine cycle (vapour power cycle) is almost unity (1.)

⊗ Brayton cycle

$$\gamma_{bw} = 0.4 \text{ to } 0.6$$

$$\gamma_w = 1 - 0.4 \Rightarrow 0.6$$

$$= 1 - 0.6 \Rightarrow 0.4$$

$$\gamma_w = 0.4 \text{ to } 0.6$$

⊗ Rankine cycle

$$\gamma_{bw} = 1 - \gamma_w$$

$$\gamma_{bw} = 1 \text{ to } 2 \%$$

$$= 0.01 \text{ to } 0.02$$

$$\gamma_w = 1 - 0.01 \Rightarrow 0.99$$

$$= 1 - 0.02 \Rightarrow 0.98$$

Note → Rankine cycle (vapour power cycle) work ratio is higher because pump are less work consume whereas Brayton cycle in compressor are more work is consume. (more power is consume)

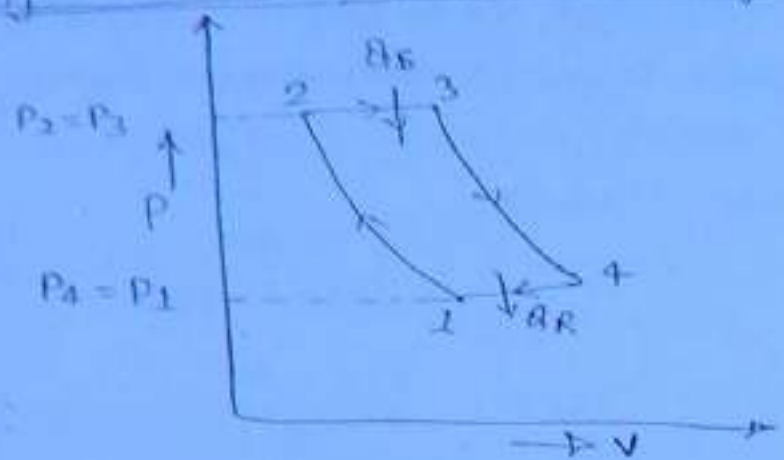
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> Efficiency of a simple gas turbine cycle on p-v diagram

$$\eta = \frac{W_{net}}{Q_s \text{ (Heat supplied)}}$$

$$\eta = \frac{Q_s - Q_R}{Q_s}$$

$$\eta = 1 - \frac{Q_R}{Q_s}$$



where $Q_R = h_4 - h_1 \Rightarrow C_p (T_4 - T_1)$

$$Q_s = h_3 - h_2 \Rightarrow C_p (T_3 - T_2)$$

$$\eta = 1 - \frac{C_p (T_4 - T_1)}{C_p (T_3 - T_2)}$$

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$$\eta = 1 - \frac{T_1 \left(\frac{T_4}{T_1} - 1 \right)}{T_2 \left(\frac{T_3}{T_2} - 1 \right)} \quad \text{--- (1)}$$

② Pressure Ratio (γ_p) = $\frac{P_2}{P_1} = \frac{P_3}{P_4}$

1-2 $\rightarrow$ Reversible adiabatic compression

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_2}{T_1} = (\gamma_p)^{\frac{\gamma-1}{\gamma}} \quad \text{--- (2)}$$

3-4 $\rightarrow$ Reversible adiabatic expansion.

$$\frac{T_3}{T_4} = \left(\frac{P_3}{P_4} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_3}{T_4} = (\gamma_p)^{\frac{\gamma-1}{\gamma}} \quad \text{--- (3)}$$

*** $\boxed{\frac{T_2}{T_1} = \frac{T_3}{T_4}}$

$$\boxed{\frac{T_4}{T_1} = \frac{T_3}{T_2}}$$

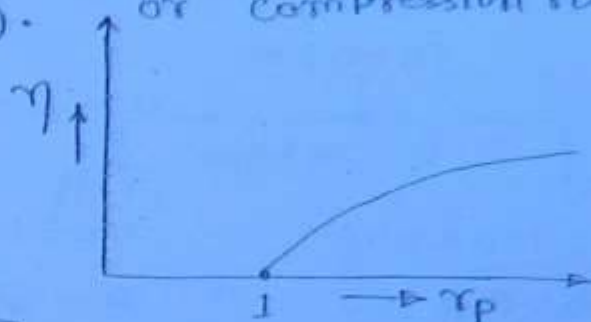
$$\eta = 1 - \frac{T_1}{T_2}$$

$$\eta = 1 - \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}}}$$

Note → For the same compression ratio, the Brayton cycle efficiency is equal to the Otto cycle efficiency.

Note → The efficiency of Brayton cycle depends on the pressure ratio (r_p) or compression ratio.

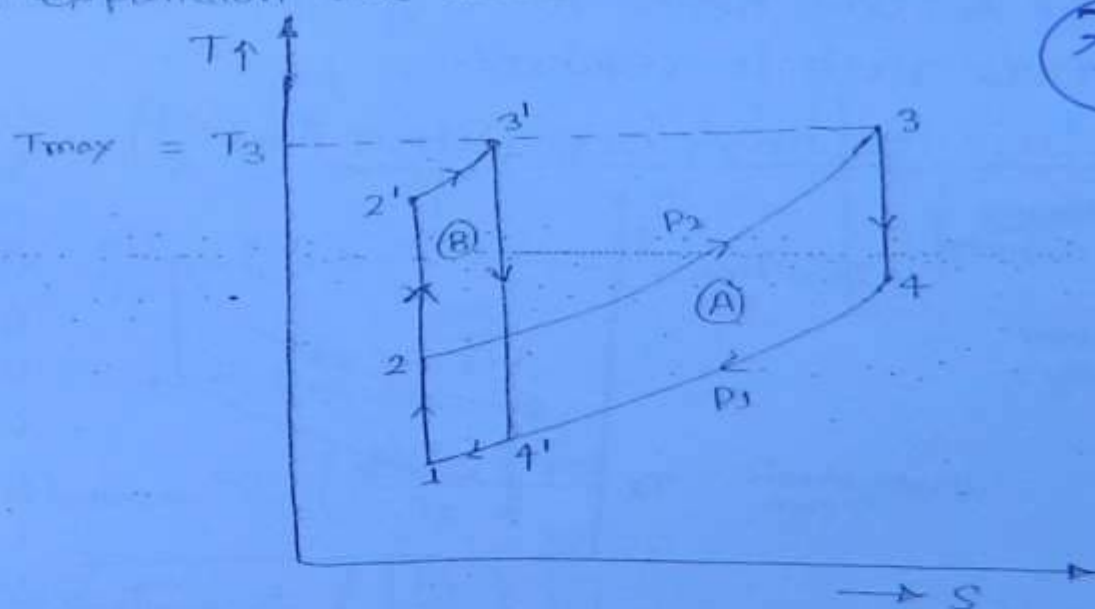
* When $r_p = 1$, then $\eta = 0$, and r_p increases then η also increases.



$$\eta = 1 - \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}}}$$

Note ⇒

This equation of η is valid only when compression and expansion are isentropic.



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$$\eta = 1 - \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}}}$$

$$\eta_B > \eta_A$$

⇒ It means efficiency depends on pressure ratio because B cycle pressure ratio is more compared to cycle A.

$W_A > W_B \rightarrow$ Area of A cycle is more compare to cycle B.
 so ^{same} mass flow rate is more than area is
 much required then cost is high. So we are not
 take more pressure ratio.
case $\rightarrow$ SAME Capacity to take.

$$\text{Power} = \dot{m} \times \text{net work}$$

1500 kW

$P = \dot{m} W_{\text{net}}$

A B

$$W_A = 150 \text{ kJ/kg}$$

$$1500 = \dot{m}_A \times 150$$

$$\dot{m}_A = 10 \text{ kg/s}$$

$$W_B = 15 \text{ kJ/kg}$$

$$P = \dot{m}_B \times 15$$

$$1500 = \dot{m}_B \times 15$$

$$\dot{m}_B = 100 \text{ kg/s}$$

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⊛ Though the efficiency of $\eta_B > \eta_A$ the net work in B $<$ cycle A and hence for a given capacity, greater mass flow rate is required.

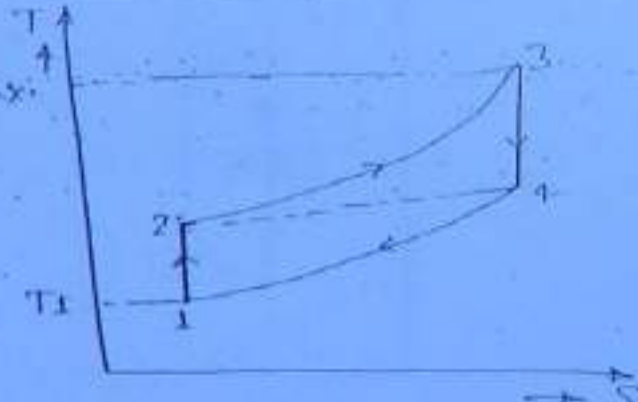
⊛ Optimum pressure for max. work output $\rightarrow$

where $T_3 \rightarrow$ Temp. constant
 because material property.

$$T_3 = T_{\text{max}}$$

$T_1, T_4 \rightarrow$ Temp. constant
 (not change)

atmospheric
Temp.



$$W_{\text{net}} = W_T - W_C$$

$$W_{\text{net}} = (h_3 - h_4) - (h_2 - h_1)$$

$$W_{\text{net}} = C_p (T_3 - T_4) - C_p (T_2 - T_1)$$

$$W_{\text{net}} = C_p (T_3 - T_4 - T_2 + T_1)$$

$$= \frac{T_2}{T_1} = \frac{T_3}{T_4}$$

$$T_2 = \frac{T_3 T_1}{T_4}$$

$$W_{net} = C_p \left[T_3 - \frac{T_1 T_3}{T_2} - T_2 + T_1 \right]$$

$$\text{For max. } W_{net} = \frac{dW_{net}}{dT_2} = 0$$

$$\frac{dW_{net}}{dT_2} = C_p \left[0 - T_1 T_3 \left(-\frac{1}{T_2^2} \right) - 1 + 0 \right] = 0$$

$$\frac{T_1 T_3}{T_2^2} - 1 = 0$$

$$T_1 T_3 = T_2^2 \Rightarrow T_2 = \sqrt{T_1 T_3}$$

$$T_4 = \frac{T_1 T_3}{\sqrt{T_1 T_3}} \Rightarrow T_4 = \sqrt{T_1 T_3}$$

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**

$$T_2 = T_4 = \sqrt{T_1 T_3}$$

Pressure ratio condition for max. work $\Rightarrow$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\text{then } \frac{P_2}{P_1} = (\gamma_p)^{\frac{\gamma-1}{\gamma}}$$

$$= \left(\frac{T_2}{T_1} \right)^{\frac{\gamma}{\gamma-1}}$$

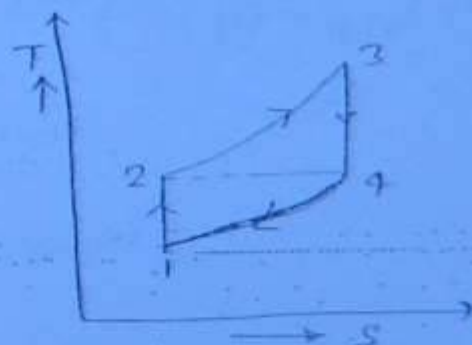
$$(\gamma_p)_{\text{optimum}} = \left(\frac{\sqrt{T_1 T_3}}{T_1} \right)^{\frac{\gamma}{\gamma-1}}$$

$$(\gamma_p)_{\text{optimum}} = \left(\sqrt{\frac{T_3}{T_1}} \right)^{\frac{\gamma}{\gamma-1}}$$

**

$$(\gamma_p)_{\text{optimum}} = \left(\frac{T_3}{T_1} \right)^{\frac{\gamma}{2(\gamma-1)}}$$

Condition for max. work

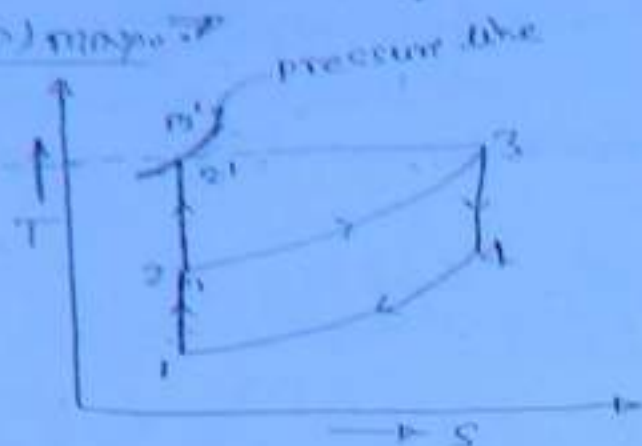


maximum pressure ratio $(\gamma_p)_{max}$

$$W_c = W_T$$

$W_{compression} = W_{expansion}$
 then net work is zero

$$W_{net} = 0$$



1-2 $\rightarrow$ Rev. adiabatic process

$$(\gamma_p)_{max} = \frac{P_2'}{P_1}$$

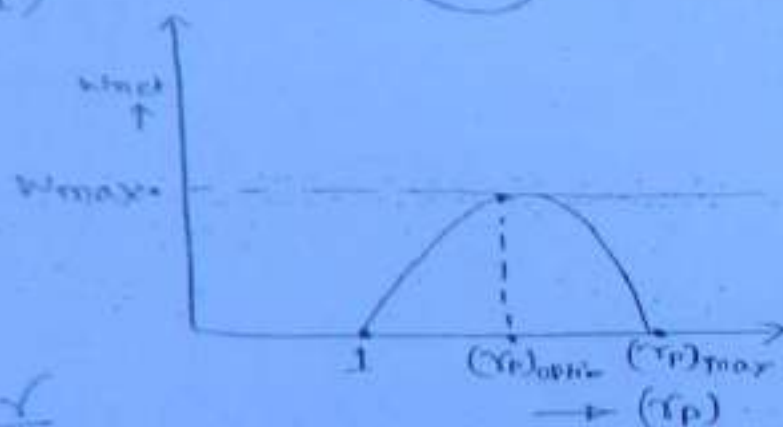
$$\frac{T_2'}{T_1} = \left(\frac{P_2'}{P_1} \right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{T_2'}{T_1} \right)^{\frac{\gamma}{\gamma-1}}$$

Because $T_2' = T_3$

$$\left(\frac{T_3}{T_1} \right) = (\gamma_p)_{max}^{\frac{\gamma-1}{\gamma}}$$

$$\frac{P_2'}{P_1} = (\gamma_p)_{max} = \left(\frac{T_3}{T_1} \right)^{\frac{\gamma}{\gamma-1}}$$

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$$(\gamma_p)_{max} = \left(\frac{T_3}{T_1} \right)^{\frac{\gamma}{\gamma-1}}$$

$$(\gamma_p)_{optimum} = \left(\frac{T_3}{T_1} \right)^{\frac{\gamma}{2(\gamma-1)}}$$

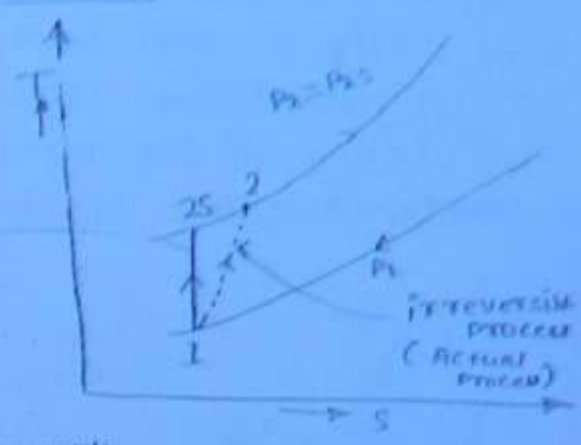
$$(\gamma_p)_{optimum}^2 = \left(\frac{T_3}{T_1} \right)^{\frac{\gamma}{\gamma-1}}$$

$$(\gamma_p)_{optimum}^2 = (\gamma_p)_{max}$$

Isentropic efficiency of a Compressor $\Rightarrow$

That means irreversible process in entropy increased.

(Isentropic line) Reversible adiabatic process



$$\eta_c = \frac{\text{Isentropic work}}{\text{Actual work}}$$

$$\eta_c = \frac{\text{Compressor work} \rightarrow \text{Less work}}{\text{Actual work} \rightarrow \text{more work}}$$

(Compressor work are less work because more power is required and turbine net work are more)

$$\eta_c = \frac{h_{2s} - h_1}{h_2 - h_1} = \frac{\text{Isentropic compression}}{\text{Actual compression}}$$

$$\eta_c = \frac{T_{2s} - T_1}{T_2 - T_1}$$

$$\frac{T_{2s}}{T_1} = \left(\frac{P_{2s}}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\left(\frac{T_{2s}}{T_1} \right) = \left(\gamma_p \right)^{\frac{\gamma-1}{\gamma}}$$

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Isentropic efficiency of a Turbine $\Rightarrow$

$$\eta_T = \frac{\text{Actual work}}{\text{Isentropic work}}$$

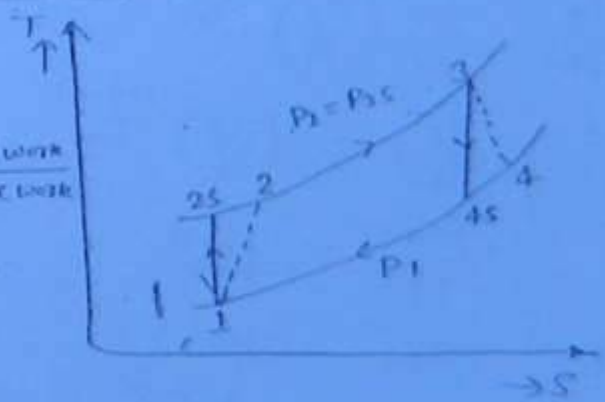
$$\eta_T = \frac{\text{Turbine actual work} \rightarrow \text{less work}}{\text{Turbine isentropic work} \rightarrow \text{more work}}$$

$$\eta_T = \frac{h_3 - h_4}{h_3 - h_{4s}}$$

$$\eta_T = \frac{T_3 - T_4}{T_3 - T_{4s}}$$

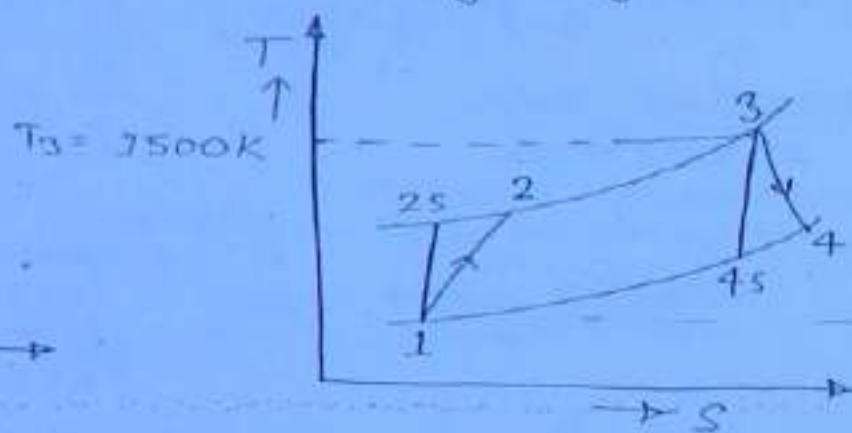
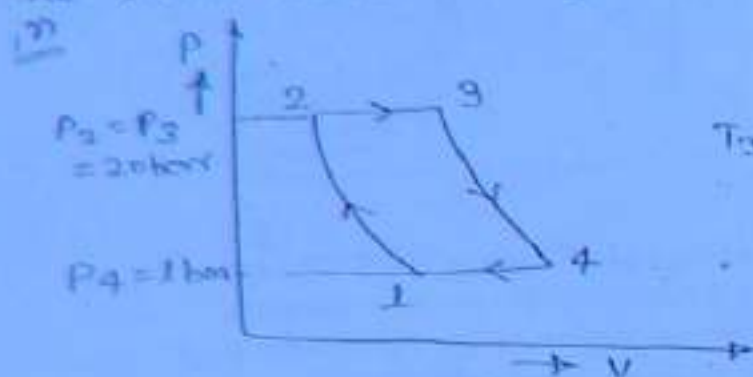
$$\frac{T_3}{T_{4s}} = \left(\frac{P_3}{P_{4s}} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\left[\frac{T_3}{T_4} = \left(\gamma_p \right)^{\frac{\gamma-1}{\gamma}} \right] **$$



Note $\Rightarrow$ Turbine work is opposite to compressor work.

Q. In a gas turbine hot combustion product with $c_p = 0.98 \text{ kJ/kg-K}$, and $c_v = 0.7538 \text{ kJ/kg-K}$ enter turbine at 20 bar, 1500K and leave at 1 bar. The isentropic efficiency of the turbine is 0.94 then find the work developed by the turbine per kg of gas.



$$c_p = 0.98 \text{ kJ/kg-K}$$

$$c_v = 0.7538 \text{ kJ/kg-K}$$

$$P_2 = P_3 = 20 \text{ bar} \quad T_3 = 1500 \text{ K}$$

$$P_4 = 1 \text{ bar} \quad \eta = 0.94 \%$$

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$$W_T = h_3 - h_4$$

$$W_T = c_p (T_3 - T_4)$$

$$\gamma = \frac{c_p}{c_v}$$

$$\gamma = \frac{0.98}{0.7538}$$

$$\frac{T_3}{T_{4s}} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_3}{T_{4s}} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_3}{T_{4s}} = \left(\frac{20}{1} \right)^{\frac{1.3-1}{1.3}}$$

$$\frac{1500}{T_{4s}} = \frac{1.99}{1}$$

$$1.99 \times T_{4s} = 1500 \times 1$$

$$T_{4s} = \frac{1500}{1.99}$$

$$T_{4s} = 751.36 \text{ K}$$

$$\eta_T = \frac{h_3 - h_4}{h_3 - h_{4s}}$$

$$\eta_T = \frac{T_3 - T_4}{T_3 - T_{4s}}$$

$$\eta_T (T_3 - T_{4s}) = T_3 - T_4$$

$$W_T = C_p (T_3 - T_4)$$

$$W_T = C_p [\eta_T (T_3 - T_{4s})]$$

$$W_T = 0.98 [0.94 (1500 - 751.36)]$$

$$W_T = 689.8 \text{ kJ/kg}$$

PROB-② air enter the compressor of a gas turbine operating on Brayton cycle at 27°C ($T_1 = 273 + 27 = 300\text{K}$). The pressure ratio is ($\frac{P_2}{P_1} = 6$). Calculate the max. Temp. in the cycle and cycle efficiency. Assume Turbine work = 2 Comp. work.
 $W_T = 2 W_C$, $\gamma = 1.4$

Soln $\gamma = 1.4$

$$W_T = 2.5 W_C$$

$$\gamma_p = \frac{P_2}{P_1} = 6$$

$$T_1 = 300\text{K}$$

$$\frac{T_2}{T_1} = (\gamma_p)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_2}{300} = (6)^{\frac{1.4-1}{1.4}}$$

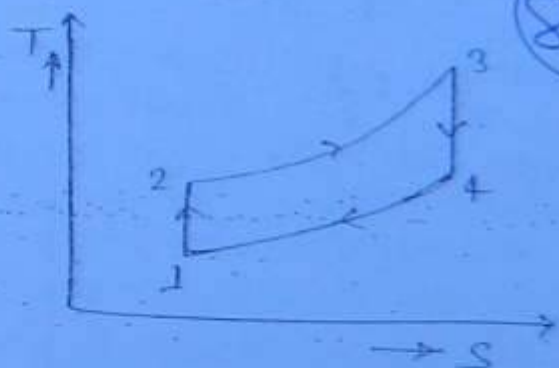
$$T_2 = 500.5\text{K}$$

$$W_T = 2.5 W_C$$

$$(h_3 - h_4) = 2.5 (h_2 - h_1)$$

$$C_p (T_3 - T_4) = 2.5 C_p (T_2 - T_1)$$

$$T_2 T_4 = \frac{T_1 T_3}{\gamma}$$



$$T_3 - \frac{T_1 T_3}{T_2} = 2.5 (T_2 - T_1)$$

$$T_3 \left(\frac{T_2 - T_1}{T_2} \right) = 2.5 (T_2 - T_1)$$

$$\frac{T_3}{T_2} = 2.5$$

$$T_3 = 2.5 \times T_2$$

$$T_3 = 2.5 \times 500.5$$

$$\boxed{T_3 = 1251.25 \text{ K}}$$

$$\eta_T = 1 - \frac{1}{(\gamma_p)^{\frac{\gamma-1}{\gamma}}}$$

$$\eta_T = 1 - \frac{1}{(6)^{\frac{1.4-1}{1.4}}}$$

$$\boxed{\eta_T = 0.4 \Rightarrow 40\%} \quad \text{Ans.}$$

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Q8. In a simple gas turbine power plant, T_1 is minimum Temp. and T_3 is the max. Temp. and what is the work ratio in terms of pressure ratio (γ_p).

Q8.

$$\eta_w = \frac{W_{net}}{W_T}$$

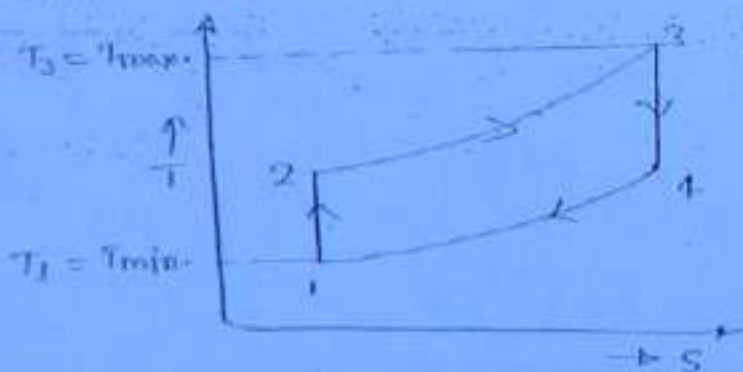
$$\eta_w = \frac{W_T - W_C}{W_T}$$

$$\eta_w = 1 - \frac{W_C}{W_T}$$

$$\eta_w = 1 - \frac{(h_2 - h_1)}{(h_3 - h_4)}$$

$$\eta_w = 1 - \frac{C_p(T_2 - T_1)}{C_p(T_3 - T_4)}$$

$$\eta_w = 1 - \frac{T_1 \left(\frac{T_2}{T_1} - 1 \right)}{T_3 \left(1 - \frac{T_4}{T_3} \right)}$$



$$\eta_w = 1 - \left(\frac{T_1}{T_3} \right) \left[\frac{(r_p)^{\frac{\gamma-1}{\gamma}} - 1}{1 - \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}}}} \right]$$

$$\boxed{\eta_w = 1 - \frac{T_1}{T_3} (r_p)^{\frac{\gamma-1}{\gamma}}} \quad \underline{\text{Ans:}}$$

PROB-④ A simple gas turbine power plant working on Brayton cycle. the power required to drive the compressor is 175 kW. Heat supplied during constant pressure heat addition is 675 kW. turbine output obtained during expansion is 425 kW. find the heat rejection.

Soln

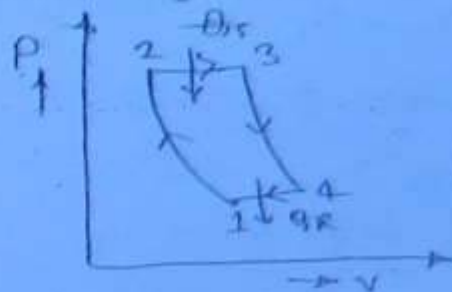
$$W_c = 175 \text{ kW}$$

$$W_{\text{net}} = Q_s - Q_R$$

$$W_t - W_c = Q_s - Q_R$$

$$425 - 175 = 675 - Q_R$$

$$\boxed{Q_R = 425} \text{ kW. } \underline{\text{Ans:}}$$



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PROB-⑤ A closed cycle gas turbine unit develop a power of 1500 kW. the pressure and temp. at the inlet to the compressor are 1 bar and 20°C. Pressure ratio is 6. the temp. to the inlet to the turbine 800°C. find the isentropic efficiency of turbine and mass flow rate of air if the isentropic efficiency of the compressor is 85% and overall efficiency is 20%. , Cp take equal to 1.005 kJ/kg·K. $\gamma = 1.4$.

Soln.

$$P = 1500 \text{ kW}$$

$$P_1 = 1 \text{ bar}$$

$$T_1 = 273 + 20 = 293 \text{ K}$$

$$r_p = 6 = \frac{P_2}{P_1}$$

$$T_3 = 273 + 800 = 1073 \text{ K}$$

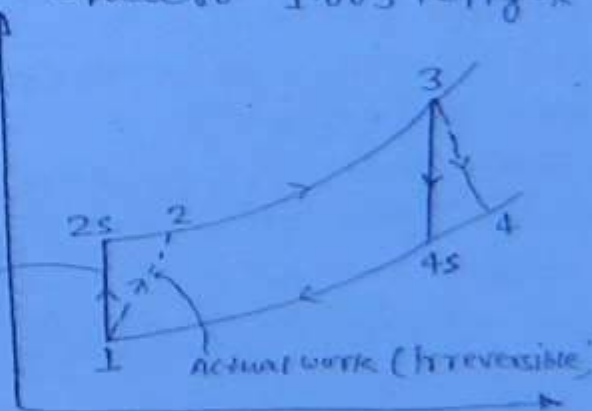
$$\eta_c = 0.85$$

$$\eta_o = 0.20$$

(Rev. adiabatic process)

Isentropic work

Actual work (Irreversible)



$$\eta_o = \frac{w_{net}}{Q_s}$$

$$\frac{T_{2s}}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_{2s}}{293} = (6)^{\frac{1.4-1}{1.4}}$$

$$\boxed{T_{2s} = 488.8 \text{ K}}$$

$$\eta_c = \frac{T_{2s} - T_1}{T_2 - T_1} \quad \begin{array}{l} \text{isentropic work} \rightarrow \text{less} \\ \text{Actual work} \rightarrow \text{more compression} \end{array}$$

$$\eta_c = \frac{488.8 - 293}{T_2 - 293}$$

$$0.85 = \frac{488.8 - 293}{T_2 - 293}$$

$$\boxed{T_2 = 523.4 \text{ K}}$$

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$$\eta_o = \frac{w_{net}}{Q_s} = \frac{w_T - w_c}{Q_s}$$

$$\eta_o = \frac{(h_3 - h_4) - (h_2 - h_1)}{h_3 - h_2}$$

$$\eta_o = \frac{C_p(T_3 - T_4) - C_p(T_2 - T_1)}{C_p(T_3 - T_2)}$$

$$0.20 = \frac{(1073 - T_4) - (523.4 - 293)}{1073 - 523.4}$$

$$\boxed{T_4 = 732.6 \text{ K}}$$

$$\frac{T_3}{T_{2s}} = \left(\frac{P_3}{P_2}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{1073}{T_{2s}} = (6)^{\frac{1.4-1}{1.4}}$$

$$T_{4s} = 643.1 \text{ K}$$

$$\eta_T = \frac{T_3 - T_4}{T_3 - T_{4s}} \rightarrow \text{less work} \quad \text{expansion}$$

$$\rightarrow \text{more work (because more ~~compression~~ decreased.)}$$

$$\eta_T = \frac{1073 - 732.6}{1073 - 643.1}$$

$$\eta_T = 79\%$$

$$(3) P = m \times W_{\text{net}}$$

$$P = m (\eta_0 \times Q_s)$$

$$\text{where } Q_s = \frac{h_3 - h_2}{}$$

$$Q_s = C_p (T_3 - T_2)$$

$$= 1.005 (1073 - 523.4)$$

$$Q_s = 552.31 \text{ KJ/kg}$$

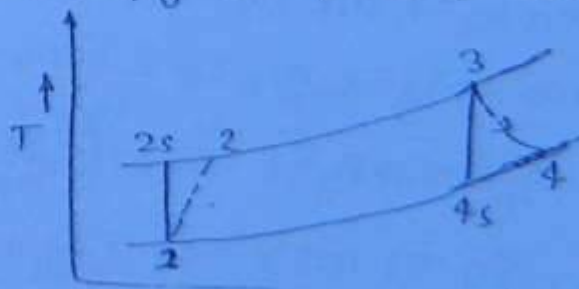
$$P = m \times W_{\text{net}}$$

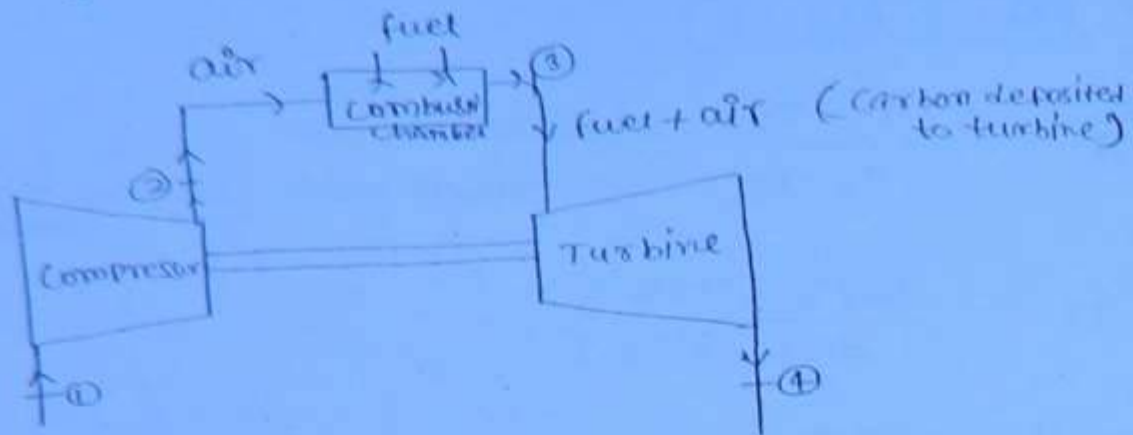
$$1500 = m (552.31 \times 0.20)$$

$$m = 13.5 \text{ kg/sec} \quad \text{Ans:}$$

PROB. (6) Air enters the compressor of a gas turbine at a bar and 293K the pressure after compression is 6 bar. Air fuel ratio 60 the isentropic efficiency of compressor and turbine are 0.84 and 0.88 respectively. Calculate the power developed by the units & its overall efficiency. Assume γ to be same for air and combustion product. take specific heat of gases = 1.1 KJ/kg-K, mass of air 5 kg/sec $C_v = 40000 \text{ KJ/kg}$.

Soln





$$T_1 = 293, \quad \gamma_p = 6$$

$$\eta_c = 0.84, \quad \eta_T = 0.88$$

$$\gamma = 1.4$$

$$\frac{T_{2s}}{T_1} = (\gamma_p)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_{2s}}{293} = (6)^{\frac{1.4-1}{1.4}}$$

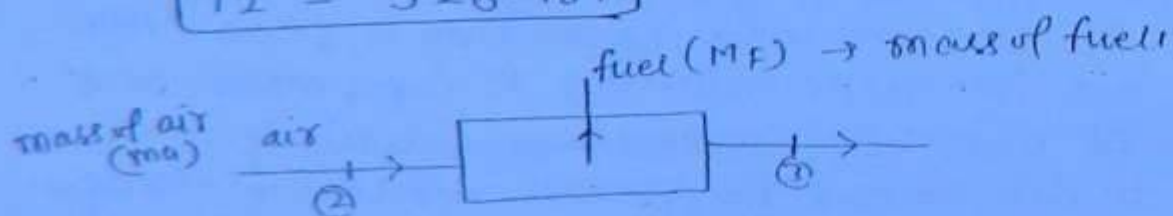
$$T_{2s} = 488.87 \text{ K}$$

90

$$\eta_c = \frac{T_{2s} - T_1}{T_2 - T_1} = \frac{\text{Isentropic work} \rightarrow \text{less}}{\text{Actual work} \rightarrow \text{more}}$$

$$0.84 = \frac{488.87 - 293}{T_2 - 293}$$

$$T_2 = 526.18 \text{ K}$$



Energy eqn.

$$m_a h_2 + m_F C_v = (m_a + m_F) h_3$$

$$m_a C_p T_2 + m_F C_v = (m_a + m_F) C_p T_3$$

$$\hookrightarrow \frac{m_a}{m_F} C_p T_2 + C_v = \left(\frac{m_a}{m_F} + 1 \right) C_p T_3$$

$$60 \times 1.005 \times 526.18 + 40000 = (60 + 1) \times 1.1 \times T_3$$

$$T_3 = 1050.3 \text{ K}$$

$$\frac{T_3}{T_{4s}} = \left(\frac{P_3}{P_{4s}} \right)^{\frac{\gamma-1}{\gamma}} = (\gamma_p)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{1059.3}{T_{4s}} = (6)^{\frac{1.4-1}{1.4}}$$

$$\boxed{T_{4s} = 635 \text{ K}}$$

$$\eta_T = \frac{T_3 - T_4}{T_3 - T_{4s}}$$

$$0.88 = \frac{1059.3 - T_4}{1059.3 - 635}$$

$$\boxed{T_4 = 685.8 \text{ K}}$$

$$W_c = \dot{m}_a (h_2 - h_1) \rightarrow \text{Compressor work}$$

$$= \dot{m}_a \times C_p (T_2 - T_1)$$

$$= 5 \times 1.005 (526.18 - 293)$$

$$\boxed{W_c = 1171.72 \text{ kW}}$$

(91)

$$\text{Turbine work } W_T = (\dot{m}_a + \dot{m}_F) (h_3 - h_4)$$

$$= (\dot{m}_a + \dot{m}_F) C_{p_{\text{gas}}} (T_3 - T_4)$$

$$= \left(5 + \frac{5}{60} \right) \times 1.11 \times (1059.3 - 685.5)$$

$$\boxed{W_T = 2107 \text{ kW}}$$

$$W_{\text{net}} = W_T - W_c$$

$$= 2107 - 1171.72$$

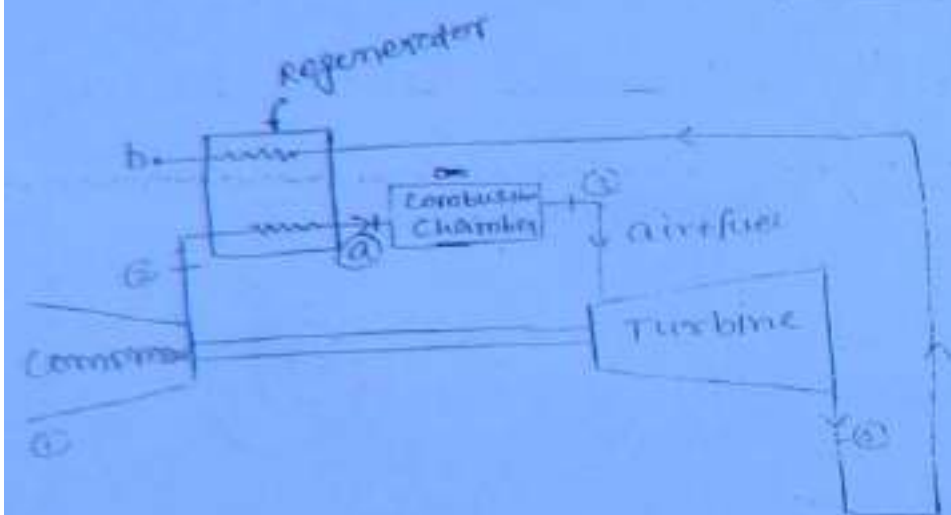
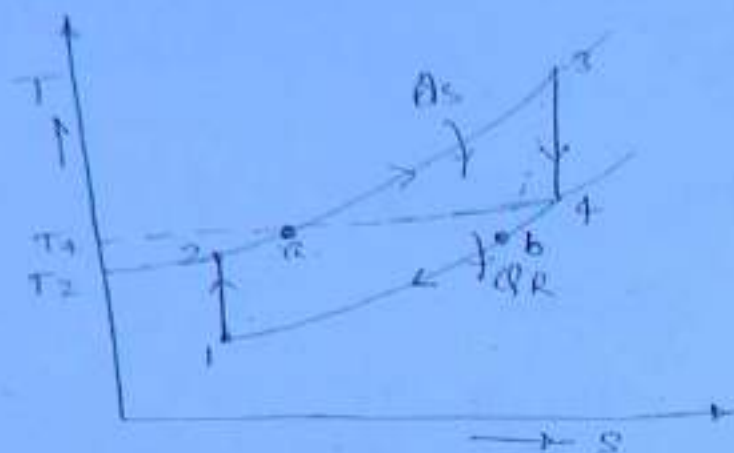
$$\boxed{W_{\text{net}} = 935.7}$$

$$Q_s = \dot{m}_F \times C_v$$

$$\eta_0 = \frac{W_{\text{net}}}{Q_s} \Rightarrow \frac{W_{\text{net}}}{\dot{m}_F \times C_v} \Rightarrow \frac{935.7}{\frac{5}{60} \times 40000}$$

$$\eta_0 = 0.2807 \quad (\text{Ans.})$$

USE OF REGENERATOR IN GAS TURBINE



(Q2)

$$\eta_p = \frac{W_{net}}{Q_s} = \frac{W_T - W_C}{Q_s} \rightarrow \text{constant}$$

when Q_s is decreases then efficiency of gas turbine increases.

effect of regeneration

- ① No change in compressor work.
- ② No change in Turbine work.
- ③ No change in Net work.
- ④ Reduction in heat supplied.
- ⑤ Increase in Turbine efficiency.

$$\eta = \frac{W_T - W_C}{Q_{sL}} \Rightarrow \frac{(h_3 - h_4) - (h_2 - h_1)}{h_3 - h_a}$$

$$\eta = \frac{C_p(T_3 - T_4) - C_p(T_2 - T_1)}{C_p(T_3 - T_a)}$$

$$\eta = \frac{T_3 - T_4 - T_2 + T_1}{T_3 - T_1}$$

⊕ effectiveness of Regenerator $\Rightarrow$

It is the ratio of Actual rise in temp. to the ideal Rise in Temperature.

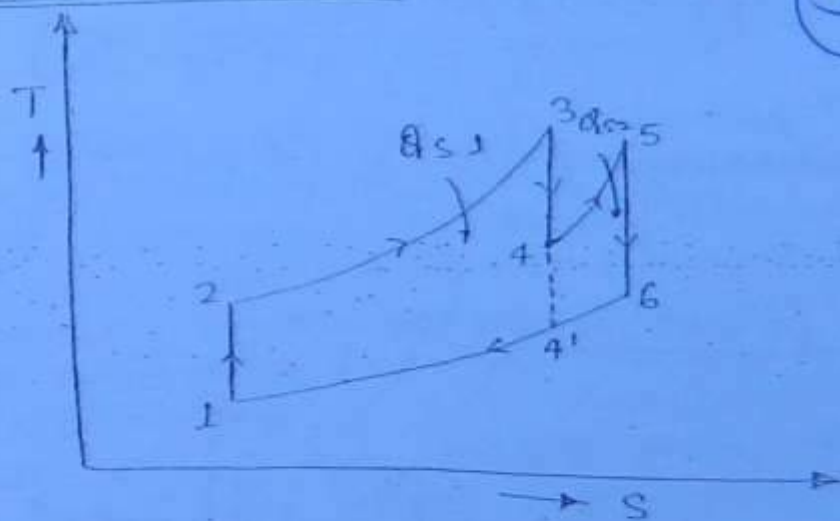
$$\epsilon = \frac{\text{Actual rise in temp.}}{\text{Ideal rise in temp.}}$$

$$\epsilon = \frac{t_a - t_2}{t_4 - t_2} \quad \text{***}$$

For effective utilisation of Regenerator the temp. difference between T_4 and T_2 should be large.

⊕ USE OF REHEATING IN GAS TURBINE $\Rightarrow$

(93)



$$W_T (\text{simple cycle}) = h_3 - h_4' = (h_3 - h_4) + (h_4 - h_4')$$

$$W_T (\text{reheat cycle}) = (h_3 - h_4) + (h_5 - h_6)$$

$$W_{\text{net}} = W_T - W_C \quad \text{when } W_C = \text{constant}$$

then W_T increase the network increase

As constant pressure line diverge

$$h_5 - h_6 > h_4 - h_4'$$

$$\therefore W_T (\text{reheat cycle}) > W_T (\text{without reheat})$$

$$\eta = \frac{W_{net} \uparrow}{Q_s \uparrow \uparrow}$$

then efficiency will be decreases.

→ with reheating the net work increases this does not mean an increase in efficiency of the cycle cause with reheating the reheat supplied is also increase th reheat because the temp $T_6 > T_4'$ and hence whenever reheating is used it is generically coupled th regeneration therefore regeneration from efficiency, increases and due to Reheating from W_{net} increases.

$$\eta = \frac{W_T - W_C}{Q_s}$$

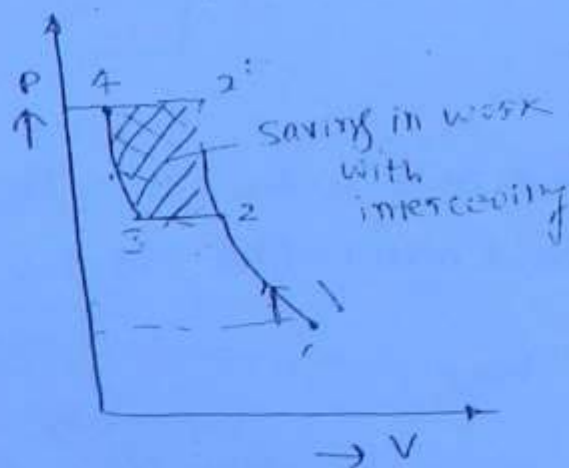
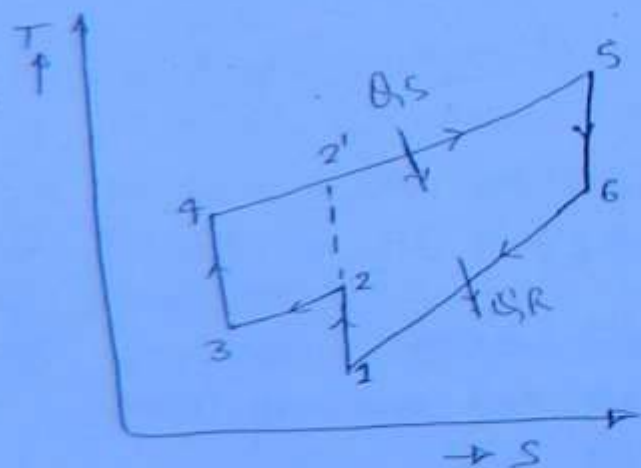
$$\eta = \frac{[(h_3 - h_4) + (h_5 - h_6)] - [h_2 - h_1]}{(h_3 - h_2) + (h_5 - h_4)}$$

$$\eta = \frac{[(T_3 - T_4) + (T_5 - T_6)] - [T_2 - T_1]}{(T_3 - T_2) + (T_5 - T_4)}$$

(94)

→ due to Reheating efficiency of the cycle decreases ↓

Intercooling in Gas Turbine →



$$W_{net} = W_T - W_C$$

$$\downarrow \eta = \frac{W_{net} \uparrow}{Q_r \uparrow}$$

⊕ Intercooling in gas turbine →

In Inter cooling the work of compression decreases and this results in increase in Net work ^{but} does not mean an increase in efficiency because the heat supplied also increases. but with intercooling the slope of for Regeneration increases because $T_4 < T_2'$ and hence intercooling is generally coupled with regeneration. →

① due to intercooling efficiency of cycle decreases (↓)

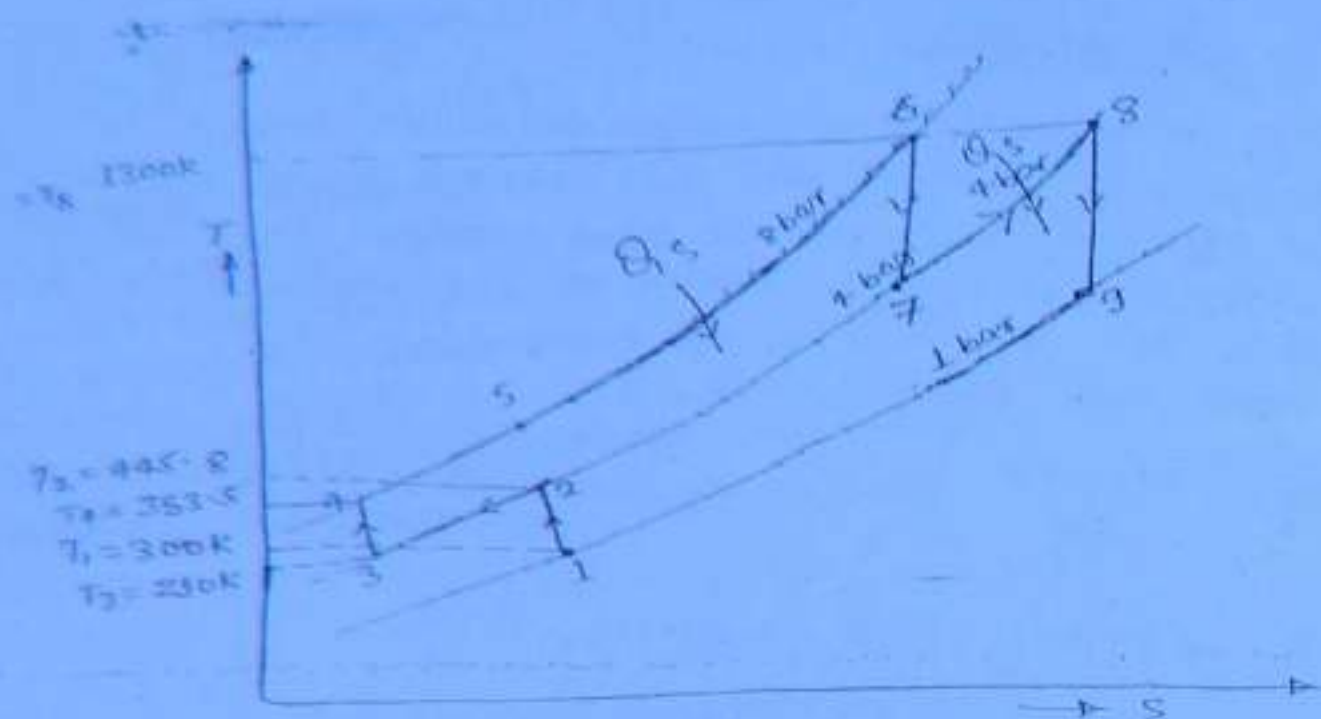
$$\eta = \frac{W_T - W_C}{Q_S}$$

$$\eta = \frac{(h_5 - h_6) - [(h_2 - h_1) + (h_4 - h_3)]}{h_5 - h_4}$$

$$\eta = \frac{(T_5 - T_6) - [(T_2 - T_1) + (T_4 - T_3)]}{T_5 - T_4}$$

95

PRCB-Q A Regenerative reheat cycle has air entering at 1 bar, 300K into the Compressor, having intercooling in between two stage of compression air leaving first stage of compression is cooled upto 290K and 4 bar pressure in intercooler and subsequently compressed to 9 bar Compressor air leaving second stage compressor is passed through a regenerator having an effectiveness of 0.8. Subsequent combustion its 1300K at inlet to the turbine having expansion upto 4 bar and then heated upto 1300K before being expanded upto 1 bar. exhaust from turbine is passed to Regenerator. Find the total turbine work and efficiency. Consider compression and expansion to be isentropic and air as the working fluid throughout the cycle.



$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_2}{300} = \left(\frac{4}{1}\right)^{\frac{1.4-1}{1.4}}$$

$$\boxed{T_2 = 445.8 \text{ K}}$$

$$\frac{T_4}{T_3} = \left(\frac{P_4}{P_3}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_4}{290} = \left(\frac{8}{4}\right)^{\frac{1.4-1}{1.4}}$$

$$\boxed{T_4 = 353.5 \text{ K}}$$

96

$$\frac{T_6}{T_7} = \left(\frac{P_6}{P_7}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{1300}{T_7} = \left(\frac{8}{4}\right)^{\frac{1.4-1}{1.4}}$$

$$\boxed{T_7 = 1066.4 \text{ K}}$$

$$\frac{T_8}{T_9} = \left(\frac{P_8}{P_9}\right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{1300}{T_9} = \left(\frac{4}{1}\right)^{\frac{1.4-1}{1.4}}$$

$$\boxed{T_9 = 874.83 \text{ K}}$$

$$\epsilon = \frac{T_5 - T_4}{T_9 - T_4}$$

$$0.8 = \frac{T_5 - 353.5}{874.83 - 353.5}$$

$$\boxed{T_5 = 770.6 \text{ K}}$$

$$W_T = (h_6 - h_7) + (h_8 - h_9)$$

$$W_T = C_p(T_6 - T_7) + C_p(T_8 - T_9)$$

$$= 1.005(1300 - 1066.4) + 1.005(1300 - 874.8)$$

$$\boxed{W_T = 662 \text{ KJ/Kg}}$$

$$\eta = \frac{W_T - W_C}{Q_S}$$

$$W_C = (h_2 - h_1) + (h_4 - h_3)$$

$$= C_p(T_2 - T_1) + C_p(T_4 - T_3)$$

$$= 1.005(445.8 - 300) + 1.005(353.5 - 290)$$

$$\boxed{W_C = 210 \text{ KJ/Kg}}$$

$$Q_S = (h_6 - h_5) + (h_8 - h_7)$$

$$Q_S = C_p(T_6 - T_5) + C_p(T_8 - T_7)$$

$$= 1.005(1300 - 770.5) + 1.005(1300 - 1066.4)$$

$$\boxed{Q_S = 766.8}$$

$$\eta = \frac{W_T - W_C}{Q_S} \Rightarrow \frac{662 - 210}{766.8}$$

$$\eta = 0.589$$

$$\boxed{\eta = 58.9\%}$$

Ans

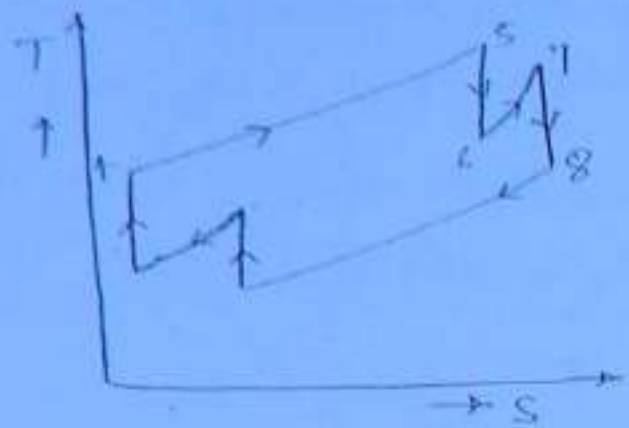
I.E.S

prob-2

The cycle shown in figure represent a gas turbine cycle with intercooling and reheating on T-s diagram.

- | | | |
|---------------------------|---|-----|
| 1. Inter cooler | → | 2-3 |
| 2. combustor | → | 4-5 |
| 3. Reheater | → | 6-7 |
| 4. High press. compressor | → | 3-4 |

match list (2)



Ques 3 The given figure shows a gas turbine cycle employing reheating on T-s diagram then find the efficiency of the cycle.

$$T_3 = 1000$$

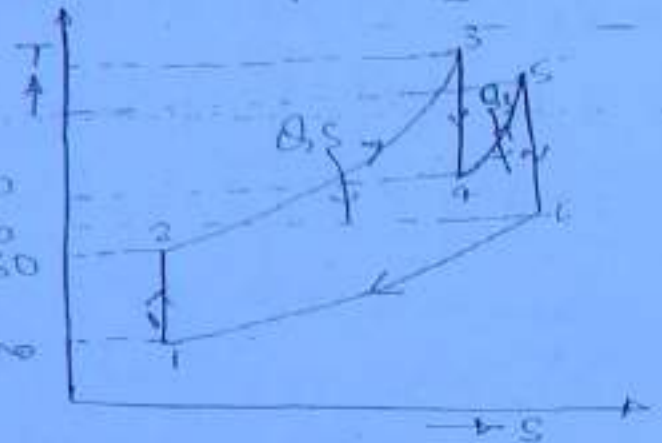
$$T_5 = 800$$

$$T_4 = 600$$

$$T_6 = 570$$

$$T_2 = 450$$

$$T_1 = 300$$



Soln

$$\eta = \frac{W_T - W_C}{Q_S}$$

$$= \frac{[(h_3 - h_4) + (h_5 - h_6)] - (h_2 - h_1)}{(h_3 - h_2) + (h_5 - h_4)}$$

$$= \frac{(T_3 - T_4) + (T_5 - T_6) - (T_2 - T_1)}{(T_3 - T_2) + (T_5 - T_4)}$$

$$\eta = \frac{(1000 - 600) + (800 - 570) - (450 - 300)}{(1000 - 450) + (800 - 600)}$$

$$\eta = 0.64 = 64\% \text{ Ans}$$

98

Prob-4 In a simple gas turbine power plant operating on standard Brayton cycle 175 kW is required to drive the compressor heat supplied during constant pressure heat addition process is 675 kW. The turbine power is 425 kW. What is the heat rejection.

Soln

$$Q_s = 675$$

$$W_T = 425$$

$$W_C = 175$$

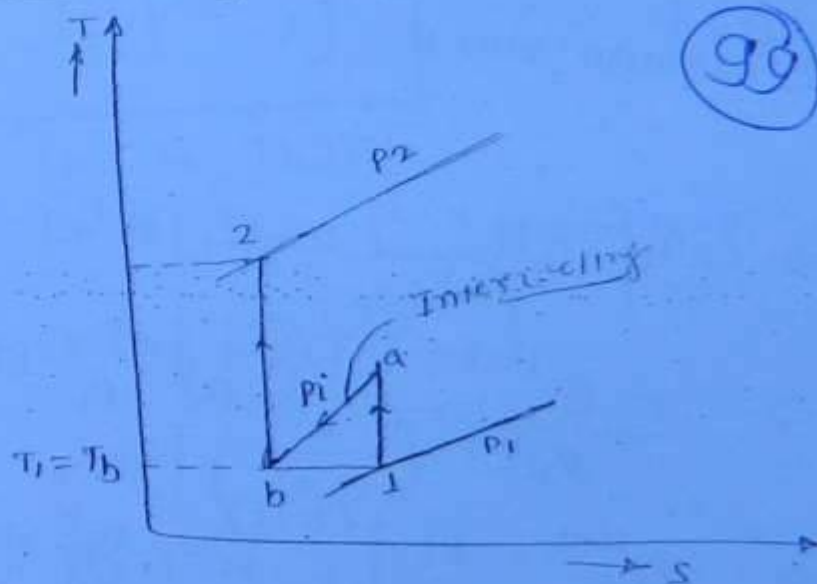
$$Q_R = ? \quad \Sigma Q = \Sigma W$$

$$Q_s - Q_R = W_T - W_C$$

$$675 - Q_R = 425 - 175$$

$$\boxed{Q_R = 425} \quad \underline{\text{Ans.}}$$

Optimum pressure ratio for min. work input $\Rightarrow$
(with perfect intercooling)



$$W_C = W_{C1} + W_{C2}$$

$$W_C = (h_a - h_1) + (h_2 - h_b)$$

$$W_C = C_p (T_a - T_1) + C_p (T_2 - T_b)$$

$$W_C = C_p [T_a - T_1 + T_2 - T_b]$$

$$W_C = C_p T_1 \left[\frac{T_a}{T_1} - 1 + \frac{T_2}{T_1} - \frac{T_b}{T_1} \right]$$

because

$$\boxed{T_b = T_1}$$

$$W_c = C_p T_1 \left[\frac{T_2}{T_1} - 1 + \frac{T_2}{T_1} - 1 \right]$$

$$W_c = C_p T_1 \left[\left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 2 + \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}} \right]$$

$$\therefore \frac{T_2}{T_1} = \frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\text{Let } \frac{\gamma-1}{\gamma} = K \quad \text{Constant}$$

$$W_c = C_p T_1 \left[\left(\frac{P_2}{P_1} \right)^K - 2 + \left(\frac{P_2}{P_1} \right)^K \right]$$

$$W_c = C_p T_1 \left[\frac{P_2^K}{P_1^K} - 2 + \frac{P_2^K}{P_1^K} \right]$$

P_1 and P_2 , C_p , T_1 , K Constant only variable P_i

For minimum work

$$\frac{dW}{dP_i} = 0$$

100

$$\Rightarrow C_p T_1 \left[\frac{K P_i^{K-1}}{P_1^K} - 0 + P_2^K (-K P_i^{-K-1}) \right]$$

$$\Rightarrow \frac{K P_i^{K-1}}{P_1^K} = K P_2^K P_i^{-(K+1)}$$

$$\Rightarrow P_i^{K-1} \cdot P_i^{K+1} = P_2^K P_1^K$$

$$P_i^{2K} = (P_1 P_2)^K$$

$$P_i^2 = P_1 P_2$$

$$P_i = \sqrt{P_1 P_2}$$

Intermediate pressure = Geometric Mean of P_1 and P_2

$P_1 \rightarrow$ Inlet ~~compressor~~ ^{pressure} for compressor 1

$$W_{C1} = W_{C2}$$

$$W_C = W_{C1} + W_{C2} = 2W_{C1}$$

$$W_C = 2C_p T_1 \left[\left(\sqrt{\frac{P_2}{P_1}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

For perfect intercooling equal work input for each compressor will be required.

$$W_{C1} = h_a - h_1$$

$$W_{C1} = C_p (T_a - T_1)$$

$$= C_p T_1 \left[\frac{T_a}{T_1} - 1 \right]$$

$$= C_p T_1 \left[\left(\frac{P_i}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

$$\text{where } P_i = \sqrt{P_1 P_2}$$

$$W_{C1} = C_p T_1 \left[\left(\frac{\sqrt{P_1} \sqrt{P_2}}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

$$W_{C1} = C_p T_1 \left[\left(\sqrt{\frac{P_2}{P_1}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

(10)

$$W_{C2} = h_2 - h_b = C_p (T_2 - T_b)$$

$$= C_p T_b \left[\frac{T_2}{T_b} - 1 \right]$$

$$\text{where } T_b = T_1$$

$$= C_p T_1 \left[\left(\frac{P_2}{P_i} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

$$= C_p T_1 \left[\left(\frac{P_2}{\sqrt{P_1 P_2}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

$$W_{C2} = C_p T_1 \left[\left(\sqrt{\frac{P_2}{P_1}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

$$W_{C2} = W_{C1}$$

$$W_C = W_{C1} + W_{C2}$$

$$W_C = 2W_{C1}$$

$$W_C = 2C_p T_1 \left[\left(\sqrt{\frac{P_2}{P_1}} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

§ Vapour Power Cycles (Rankine Cycle)

Reason for using water as a working fluid in vapour power cycle.

1. It is cheap.

2. It is chemically stable.

3. It is harmless substance.

§ specific steam consumption $\rightarrow$

$$SSC = \frac{\text{mass of steam}}{P_{\text{net}}} = \frac{m_s \rightarrow \text{kg/s}}{P_{\text{net}} \rightarrow \text{KJ/sec.}}$$

$$SSC = \frac{m_s \rightarrow \text{kg/s}}{m_s \times W_{\text{net}} \rightarrow \text{KJ/kg}}$$

$$SSC = \frac{1}{W_{\text{net}}} \text{ KJ/kg} \Rightarrow \frac{\text{kg}}{W_{\text{net}} \cdot \text{KJ}}$$

$$SSC = \frac{\text{kg}}{W_{\text{net}} \frac{\text{KJ} \times \text{sec}}{\text{sec}}}$$

$$SSC = \frac{\text{kg}}{W_{\text{net}} \text{ KW-sec}}$$

$$SSC = \frac{\text{kg}}{W_{\text{net}} \text{ KW} \times \frac{1}{3600} \text{ hr}} \quad \begin{matrix} 1 \text{ hr} = 3600 \text{ sec} \\ 1 \text{ sec} = \frac{1}{3600} \text{ hr} \end{matrix}$$

$$SSC = \frac{3600 \text{ kg}}{W_{\text{net}} \text{ KW-hr}}$$

If the net work is more specific steam consumption is less and hence mass flow rate of steam will be less and hence the size of the plant will be small.

§ CARNOT CYCLES $\rightarrow$

$$W_{\text{net}} = W_T - W_C$$

